Correlation analysis and partial least square modeling to quantify typical minerals with Chang'E-3 visible and near-infrared imaging spectrometer's ground validation data

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Abstract In 2013, Chang'E-3 program will develop lunar mineral resources in-situ detection. A Visible and Near-infrared Imaging Spectrometer (VNIS) has been selected as one payload of CE-3 lunar rover to achieve this goal. It is critical and urgent to evaluate VNIS' spectrum data quality and validate quantification methods for mineral composition before its launch. Ground validation experiment of VNIS was carried out to complete the two goals, by simulating CE-3 lunar rover's detection environment on lunar surface in the laboratory. Based on the hyperspectral reflectance data derived, Correlation Analysis and Partial Least Square (CA-PLS) algorithm is applied to predict abundance of four lunar typical minerals (pyroxene, plagioclase, ilmenite and olivine) in their mixture. We firstly selected a set of VNIS' spectral parameters which highly correlated with minerals' abundance by correlation analysis (CA), and then stepwise regression method was used to find out spectral parameters which make the largest contributions to the mineral contents. At last, functions were derived to link minerals' abundance and spectral parameters by partial least square (PLS) algorithm. Not considering the effect of maturity, agglutinate and Fe^0 , we found that there are wonderful correlations between these four minerals and VNIS' spectral parameters, e.g. the abundance of pyroxene correlates positively with the mixture's absorption depth, the value of absorption depth added as the increasing of pyroxene's abundance. But the abundance of plagioclase correlates negatively with the spectral parameters of band ratio, the value of band ratio would decrease when the abundance of plagioclase increased. Similar to plagioclase, the abundance of ilmenite and olivine has a negative correlation with the mixture's reflectance data, if the abundance of ilmenite or olivine increase, the reflectance values of the mixture will decrease. Through model validation, better estimates of pyroxene, plagioclase and ilmenite's abundances are given. It is concluded that VNIS has the capability to be applied on lunar minerals' identification, and CA-PLS algorithm has the potential to be used on lunar surface's in-situ detection for minerals' abundance prediction.

Key words Lunar surface; Chang'E-3; VNIS; partial least square (PLS)

1 Introduction

Mineral composition and distribution of lunar surface is critical for investigating the origin and geologic evolution of the Moon. e.g. the mineralogy information of craters' ejecta can be used to investigate lunar crustal structure (Tompkins and Pieters, 1999; Joliff et al., 2000; Pieters, 1993; Williams et al., 1995; Cahill et al., 2009). Besides, the mineral distribution of lunar surface will help us improve the hypothesis of 'magma ocean' (Wood, 1975; Solomon and Longhi, 1977; Elkins-Tanton et al., 2002). The second phase of Chang'E Program (Chang'E-3) is to land and perform *in-situ* detection on lunar surface. And one of the scientific goals of Chang'E-3 is to develop lunar mineral resources survey and composition *in-situ* detection (Ouyang Ziyuan, 2005). To achieve this goal, a VIS/NIR imaging spectrometer (VNIS) based on Acousto-Optic Tunable Filter (AOTF) technique has been selected as a payload of Chang'E-3 lunar rover (He Zhiping et al., 2011), main parameters of VNIS is listed in Table 1. Chang'E-3 would be the first mission to carry on hyperspectral imaging spectrometer for lunar *in-situ* detection, the detection mode and data processing methods will be different from that of ground-based telescopes and satellites.

VNIS has become an effective approach to character and predict abundance of lunar minerals and elements (Ling Zongcheng et al., 2010, 2011a, b; Yan Bokun et al., 2012; Lucey, 2004). Three kinds of prediction approach are commonly used. The first one is statistical model based on the links between spectral parameters and the mineral constitutes, such as multiple linear regression model (MLR) (Shkuratov et al., 2003, 2005a, b; 2007), principal component regression (PCR) (Pieters et al., 2002; Zhang Xiaoyu, 2008), and partial least square (PLS) regression (Li Lin, 2006, 2007, 2008, 2010; Li Shuai and Li Lin, 2011, 2012). The second approach is modified Gaussian model (MGM) (Sunshine et al., 1990, 1993, 1998; Nobel et al., 2000, 2005), which is a common method to fit mineral absorption features based on Gauss curves. The last one is radiative transfer models (Cahill et al., 2007, 2010; Denevi et al., 2008; Li Lin and Li Shuai, 2010; Lucay, 2004; Wilcox et al., 2006), which has taken physical factors (e.g. the particle size, the maturity and the porosity) into account. All methods referenced above have been applied to evaluate lunar soils' composition, but there are limitations for each one. The disadvantage of radiative transfer model is that the model is too complex and it is difficult to obtain pure end-member spectra. MGM is timeconsuming and only effective to the minerals (e.g. pyroxene or olivine) whose absorption features are obvious.

Compared with the other two methods' limitations, statistical analysis methods based on the links between spectral parameters and mineral composition are widely used for its convenience. In contrast to MLR and PCR (Shkuratov et al., 2003; Pieters et al., 2002, 2006), PLS algorithm (Li Lin, 2006) has the advantage of fewer components used and higher precision. Nevertheless, defects also exist in PLS model (Li Shuai et al., 2012). First of all, PLS algorithm makes all the bands participated in the model establishment, making effective removal of redundant spectral bands very hard. Then, nonlinear spectral mixing is not considered in the process. To solve these two problems, GA-PLS and PLS-BPNN algorithms are introduced (Li Lin and Li Shuai, 2010; Li Shuai et al., 2012), GA-PLS selects effectively a series of spectral features data which provide the largest contribution to mineral inversion, while neglect the nonlinear spectral mixing factors. After that, PLS-BPNN algorithm is developed to overcome these two limitations and better results are derived. But it is noticeable that a sufficient number of training samples are needed for PLS-BPNN algorithm to achieve a stable estimation, which should also cover the full range of compositions and physical properties (Li Shuai et al., 2012). Based on previous works, the focus of the study is to establish a new PLS model combined with correlation analysis (CA-PLS), which is an effective way for selecting a set of effective spectral parameters data to predict mineral abundance. Using the ground validation experiment data of VNIS, a set of VNIS' spectral parameters highly correlated with minerals' abundance were found through correlation analysis, then the Stepwise Regression Analysis method was used to find out spectral parameters which makes the largest contributions to the mineral contents. At last, functions are derived to link minerals' abundance and the selected spectral parameters by PLS.

2 Data description

2.1 Ground validation experiment of VNIS

Before the launch of CE-3 lunar rover, lots of ground validation experiments need to be done for VNIS and other payloads. The purpose of ground validation experiment is to understand the performance of the instruments, evaluate data quality and practice data processing methods. There are two objectives of VNIS ground validation experiment, one is to simulate VNIS' working conditions on lunar rover and evaluate its image and spectrum data quality, another is to build up minerals' prediction models according to the spectral data of seven mixtures composed of different minerals' proportion. The experiment pipeline is shown in Fig. 1, and Fig. 2 demonstrates the devices and measurement principle. During the process of ground validation experiment, VNIS is compared with a standard spectrometer named ASD, and these two spectrometers were fixed on the simulated lunar rover at the same viewing geometry. The type of ASD we used is Field Spec 3, the performance and specification could be known from http://www.asdi.com. Calibration target was firstly detected by VNIS and ASD at the same time and the same geometry. After that, experiment samples were changed to be detected until all the samples finished detection. The working geometry is as follow: the incident angle of light sources was fixed at 60°, and the detection angle of VNIS and ASD was fixed at 45°, the azimuth angle between lunar rover and light sources is 180°.

	able 1 Main parameter of VNIS	
Spectral range	450–2400 nm	
Spectral resolution	≤8nm @450–950 nm, ≤12nm @950–2400 nm	
Band	100@450-950 nm, 300 @950-2400 nm	
Corresponding RF frequency	40–180 Mhz	
Field of view	$\geq 6^{\circ} \times 6^{\circ}$ (VIS), 3°×3°(NIR)	
Wavelength selection	Continuously tunable	
Image signal-to-noise ratio	\geq 30	

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2.2 Samples preparation

During VNIS ground validation experiment in the laboratory, we tried our best to simulate its working conditions on lunar surface. Nevertheless, it turned out to be very difficult to simulate lunar soils completely, especially the maturity and composition. Five kinds of mineral whose spectral features are obvious and close to lunar minerals were selected as raw experiment samples, namely, hyperthene, diopside, olivine, plagioclase and ilmenite. These minerals were firstly ground by the grinder and the median particle sizes were controlled at the range of 40-130 µm, simulating the median particle sizes on lunar surfaces. Major chemical analysis of the minerals is listed in Table 2 except ilmenite, the composition of which is mainly TiO₂. The bidirectional-hemispheric reflectance data of the five minerals were measured in the laboratory by standard spectrophotometer (Fig. 3). Then hyperthene, olivine, plagioclase and ilmenite were selected to be stirred and mixed as the seven proportions provided by Table 4, and these seven mixtures are final samples used for ground validation experiment, which aims to evaluate VNIS spectral data quality and practice mineral quantification method. Hyperthene is selected other than diopside for the reason that the spectrum of hyperthene is similar to the pyroxene on lunar surface.

2.3 Data processing

This section contained VNIS and ASD data processing. The steps and pipeline of VNIS data processing are shown in Fig. 7, and dark current subtraction, radiance calibration and reflectance conversion are included. VNIS measured dark current data before and after sample detection, so the mean values of the dark current data could be subtracted when the detection finished. After dark current subtraction, radiance calibration is needed to change the raw data to radiance using coefficients, that were derived from the radiance calibration experiment of Shanghai Institute of Technical Physics, from pre-flight radiance calibration experiment. At last, reflectance conversion must be done because reflectance data reflects the characters of the minerals and is fundamental for mineral prediction models' establishment. We could calculate VNIS bidirectional reflectance factor (BRF) data with the methods employed by Mars' Pathfinder, Sprit and Opportunity (Reid et al., 1999; Bell et al., 2003, 2006).



Fig. 1. VNIS' ground validation experiment pipeline.



Fig. 2. Experiment devices and measurement principle.



Fig. 3. Bidirectional-hemispheric reflectance features of the five minerals in the laboratory.

Table 2 Chemical composition measured for the raw mineral												
Mineral	SiO ₂	TiO ₂	Al_2O_3	Cr_2O_3	FeO	NiO	MnO	MgO	CaO	Na ₂ O	K_2O	Total
Hyperthene	53.64	0.12	3.72	0.23	17.31	0.04	0.29	24.73	0.49	0.02	0.01	100.60
Diopside	55.72	0.08	0.16	0.53	1.24	0.02	0.06	17.22	24.45	0.37	0.01	99.86
Olivine	41.89	0.02	0.02	0.01	8.62	0.38	0.13	49.18	0.06	0.02	0.01	100.31
Plagioclase	56.14	0.03	27.62	0.01	0.08	0.01	0.01	0.02	10.44	5.13	0.37	99.87

Table 3Mineral proportion of seven mixture							
No.	Mineral proportion (wt.%)						
	Hyperthene	Olivine	Plagioclase	Ilmenite			
Mixture 1	10	20	30	40			
Mixture 2	40	30	20	10			
Mixture 3	20	40	10	30			
Mixture 4	30	10	40	20			
Mixture 5	45	0	50	5			
Mixture 6	60	5	35	0			
Mixture 7	0	15	70	15			



Fig. 4. The final mixture samples prepared for the experiment (from left to right, mixture 1 to 7).



Fig. 5. VNIS' ground data processing pipeline.

The steps of ASD data processing are similar to that of VNIS, which also contained three steps: dark current subtraction, radiance calibration and reflectance conversion. The reflectance spectrum of seven mixtures obtained by VNIS and ASD under the same conditions is plotted in Fig. 8. We can concluded that the shape and values of VNIS reflectance is close to that of ASD from Fig. 8 a and c, which demonstrate that the quality of VNIS spectral data is well and absorption features of minerals can be characterized effectively. But Fig. 8a also demonstrates that there is stronger spectral jitter in VNIS spectral range of 450–900 nm than other wavelengths. This is mainly caused by the reason that the intensity of light source in the laboratory is weaker than sunlight in the spectral range of 450-950 nm, and the bands' integrating time parameters of VNIS' detector (CCD) in this spectral range are set as the intensity of sunlight, which lead to the intensity every band received is weak, so VNIS signal to noise ratio (SNR) was brought down. To remove this spectral jitter, five-point linear smoothing algorithm was used to VNIS' original reflectance data (Fig. 8b), and the data after smoothed was used to establish models for minerals' prediction.

3 CA-PLS model description and application

Three steps are needed for CA-PLS to predict mineral abundance in the mixture, they are correlation analysis, stepwise regression analysis and PLS modeling.

3.1 Correlation analysis and stepwise regression

Correlation analysis (CA) is a simple and effective statistical approach which analysis the closeness between two correlated variables, which is expressed as correlation coefficient. There are three kinds of correlation coefficients, Pearson, Spearman and Kendall. Pearson correlation coefficientis can be calculated by the following formula:

$$r = \frac{N \sum x_i y_i - \sum x_i \sum y_i}{\sqrt{N \sum x_i^2 - (\sum x_i)^2} \sqrt{N \sum y_i^2 - (\sum y_i)^2}}$$
(1)

where r is Pearson correlation coefficient, N is the number of samples data, x_i and y_i represent the two variables, spectral parameter and mineral's proportion in the mixture, respectively.

VNIS is a hyperspectral instrument which contained 400 bands. High correlation existed among these bands' reflectance, so CA is firstly used to select a set of bands' reflectance and spectral parameters data as the independent variables show high correlation with the dependent ones of mineral contents in the mixture. Then, Stepwise Regression Analysis is applied to find out five bands' reflectance or spectral parameters which make the largest contributions to the mineral contents. The five bands' reflectance or spectral parameters data selected will be involved in the PLS model establishment.



Fig. 6. Reflectance features comparison of VNIS and ASD for the seven mixtures. (a) Reflectance data obtained by VNIS; (b) reflectance data obtained by VNIS smoothed by five-point linear smoothing algorithm; (c) reflectance data obtained by ASD (There is a conjunction between ASD two detectors near 1000 nm, so there is a spectral at some wavelengths near 1000 nm).

The spectral parameters included bands' reflectance, band ratio (or color index), absorption depth and bend data. Band ratio is the ratio of two bands' reflectance, absorption depth is the distance between the lower point of the wave trough to the normalized envelope (Fig. 7), and the parameter of bend to character the absorption feature near 1000 nm is defined by Pieters et al.(2006).



$$band _ratio = \frac{band _\lambda_2}{band \ \lambda_1}$$
(2)

Absorption _ depth =
$$\rho - \rho_m =$$

 $\rho_2 + \frac{(\lambda_2 - \lambda_m)(\rho_1 - \rho_2)}{\lambda_2 - \lambda_1} - \rho_m$
(3)

$$Bend = \frac{band \, \lambda_1 \times band \, \lambda_m}{\left(band \, \left(\lambda_1 + \lambda_m\right)/2\right)^2} \tag{4}$$

The spectral absorption features of the seven mixtures are mainly existed near 1000 and 2000 nm. As the absorption depth defined in Figure 7, when calculating the above spectral parameters, we need to specify the beginning band, the trough band and the end band of the seven mixtures' absorption. So the bands of beginning, trough and end of the absorption near 1000 nm are λ_1 =705 nm, λ_m =905 nm, λ_2 =1105 nm, and for the absorption of 2000nm, bands of the beginning, trough and end of the absorption are λ_1 =1555 nm, λ_m =1955 nm, λ_2 =2350 nm.

3.2 PLS modeling

Partial Least Square (PLS) is a powerful regression method which helps to set up relationships between mineral composition and spectral parameters. The details of the algorithm have been described by Li Lin (2006). The advantages of PLS are as follow:

(1) Regression modeling can be made under the condition of the independent variables' multiple correlation.

(2) Regression modeling is allowed under the condition that the number of sample data is less than number of independent variables.

(3) The final regression model will contain all of the original variables.

Due to the limitation of sample's amount, the number of the dependent variables (only seven abundance data for every mineral) is far less than the independent variables (400 bands reflectance data and other spectral parameters), so PLS algorithm was selected and used to establish relationship between dependent variables (the mineral abundance in the mixture) and independent variables (spectral parameter data). The final model formula is as follow:

$$\frac{Mineral_abun = c_0 + c_1 \times Spec_p_1 + c_2 \times Spec}{p_2 + c_3 \times Spec_p_3 + \dots + c_n \times Spec_p_n}$$
(5)

where *Mineral_abun* is one kind of mineral abundance, $Spec_p_1$, $Spec_p_2$, $Spec_p_3$, ..., $Spec_p_n$ are spectral parameters, and c_0 , c_1 , c_2 , c_3 , c_n are regression coefficient.

Root mean square error (RMSE) is used to demonstrate the model accuracy, and the relative prediction error (δ) is calculated to indicate which minerals can be predicted better.

$$RMSE = \sqrt{\sum_{i=1}^{n} (y_i' - y_i)^2 / (n-1)}$$
(6)

$$\delta = \frac{RMSE}{\overline{M}} \times 100\% \tag{7}$$

where *n* is the number of samples, here n=7, *i* is the index of the sample, y_i is mineral prediction value, y_i is the actual mineral relative abundance in the mixture, and *M* is mean mineral abundance value of all the seven samples.

4 Results and discussion

The prediction results of the four minerals are acquired, every mineral's five final spectral parameters are selected after correlation analysis and stepwise regression, and the prediction coefficients are derived by PLS modeling. During the process of the four minerals' modeling, we selected five of the seven mixture's spectral and composition data as training data, the other two mixtures' spectral and composition data were validation data. The four minerals' model equations are as follow.

4.1 Pyroxene model

The pyroxene abundance of five training data has significant correlation with many spectral parameters. For example, the correlation coefficients between pyroxene contents and absorption_depth_1000, 2000,

band ratio 900/750 nm, bend_1000, 2000 nm are higher than 92%. As the proportion of pyroxene raised, the absorption depth of 1000 and 2000 nm would increase. The five spectral parameters were selected as independent variables. And the PLS model quantifying pyroxene content in the mixture is as follow:

4.2 Plagioclase model

Plagioclase abundance data correlated highly with the spectral parameters of band ratios. As the proportion of plagioclase increased, the values of band ratios would decrease. We selected five band ratio parameters as independent variables, and set up a PLS model to quantify plagioclase contents in the mixture.

4.3 Olivine model

Olivine abundance correlated highly with some band reflectance data. As the proportion of olivine grew, the values of band reflectance would decrease. We selected five bands reflectance by correlation analysis and stepwise regression as independent variables, and established the PLS model to quantify olivine contents in the mixture.

Olivine=76.458+1871.693× (band_500)-1651.318×(band_690)+592.573× (band_745)-1185.73×(band_830)+ 302.322×(band_1000) (10)

4.4 Ilmenite model

Ilmenite composition correlated highly with band reflectance data. As the proportion of ilmenite went up, the values of band reflectance would decrease. We selected five band reflectance data as independent variables, and set up a PLS model to quantify ilmenite contents in the mixture.

Ilmenite=61.755+163.522×(band_1050)+ 226.069×(band_1550)+480.772×(band_1750) -728.384×(band_2000)-229.824×(band_2350) (11)



Fig. 8. Comparison of the four minerals abundance with those predicted from CA-PLS model. (a) Pyroxene model: mixture 3 and 5 were validation data, and the other five are training data; (b) plagioclase model: mixture 2 and 6 were validation data, and the other five are training data; (c) olivine model: mixture 1 and 4 were validation data, and the other five are training data; (d) ilmenite model: mixture 2 and 4 were validation data, and the other five are training data;

Comparison of the four minerals abundance with those predicted from CA-PLS model are shown in Fig. 8. The training samples are represented by open circles, while the validation sample are characterized by the solid dots. The sold line is 1:1 correlation line.

 Table 4
 The RMSE and relative errors calculated in the prediction of the four mineral abundance

Mineral component	PLS prediction					
winierar component	RMSE	Relative error (%)				
Hyperthene	0.04	13.79				
Plagioclase	0.03	8.33				
Olivine	0.13	75.85				
Ilmenite	0.03	17.5				

The RMSE and relative prediction errors are listed in Table 4. Generally speaking, the prediction results of hyperthene and plagioclase are satisfactory with the low level of RMSE (0.04 and 0.03), and the relative prediction errors are small for the values of 13.79% and 8.33%. The prediction result of ilmenite is passable, with the values of RMSE and relative error are 0.03% and 17.5%. But the prediction result of olivine is undesirable, with the highest relative error value of 75.87%.

The undesirable result of olivine prediction is mainly caused by the following reasons: (1) correlation between olivine abundance and spectral parameters is not so significant as that of other minerals, which makes the olivine's prediction model is not precise; (2) The number of training data for statistical analysis is only five groups, the estimation results of which may be stable but they are unlikely optimal, the additional samples which extend the abundance range of training data may improve the prediction results. In this experiment, the amount of our sample is limited and the size of our sample must cover VNIS field of view, so we have to make seven mixtures. (3) the models still not consider non-linear spectrum effect between the spectral parameters and the abundance data.

5 Conclusions

Take advantage of seven mixtures' spectral data and mineral composition data, correlation analysis and partial least square algorithm were used to set up four minerals abundance prediction models. The root mean square errors and relative prediction errors were calculated to evaluate the accuracy. Results demonstrate that the models can well predict pyroxene, plagioclase and ilmenite's abundance, while the results of olivine are not desirable, which was further discussed.

More work is still needed to evaluate VNIS' capability and improve the algorithm under study. Non-linear spectrum effect will be considered in the future. The main purpose of this paper is to evaluate the spectral data quality of VNIS and validate the CA-PLS prediction algorithm. The landing site of CE-3 lunar rover has been selected in the district of Sinus Iridum, which is an impact basin filled with basalt. Considering the difference between our ground validation sample and lunar real soils, CA-PLS algorithm will be used to set up lunar minerals' prediction models which are suitable for VNIS' bands based on the lunar highland and mare soils' reflectance and composition data characterized by the Lunar Soil Characterizations Consortium (LSCC). In conclusion, VNIS is not only can be used to distinguish the lunar main minerals, CA-PLS algorithm also has the potential to predict lunar minerals' abundance.

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